

# Simulation Model on Chaotic Asynchronous Transmitter and Receiver

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In this research project a new method for secure information transmission, a chaotic communication system, is designed and presented. The architecture of the communication system is constructed using Rössler's attractor of three differential equations for a transmitter, receiver and the error system. The information to be transmitted is concealed in the solutions to Rössler's equations. This allows for the secure transmission of the information. These solutions are then transmitted to a receiver designed to extract the information from the solutions. Simulation results demonstrate the proof of concept of secure transmissions via this method.

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## Introduction

Network users have become critically concerned about security levels of information systems wiring up their electronic devices, due to the rapid increase of values of their transactions and communication. Security is now playing an essential role in the growth of electronic businesses and the functioning of the whole economy. In fact, according to statistics research by Ponemon Institute LLC [1], more than 43% of companies experienced data breach in 2013. This resulted in a tremendous economic loss for individuals and corporations.

Information security issues encouraged researchers to seek means of data transmission with higher security levels, and they turned to chaos theory. Being one of the three greatest scientific revolution on the 20<sup>th</sup> century [2], chaos theory was a study of non-linear complex, dynamic systems. The basic principle of chaos theory is that even in an entirely deterministic system, the slightest change in the initial data can cause abrupt and seemingly random change in the outcomes.

Development breakthroughs in chaos theory such as Chua's Circuit (1983), a simple electronic circuit that exhibits classic chaos signal, and the realization of a synchronized coupled system in 1990 by Louis M. Pecora and Thomas L. Carroll, marked great milestones in the development of chaos theory. Many heads were turned for the synchronization of chaos, which could be applied to transmitting information signals in a secure design, developing a new branch of chaos theory, chaos communication. Since then, chaos theory has been playing a significant role for transmitting secure information signals.

- **Chaos communications system**

Chaos communication, a branch application of chaos theory, was aimed to provide security in information transmission.

Chaos signals, used as a carrier waveform for information transmission, holds unique features for encrypting data signals for the transmission process, including complex behavior, noise-like dynamics (pseudorandom noise) and spread spectrum [3]. These characteristics make chaotic signal an ideal carrier for data transmission.

The type of chaos secure communication method used in this study is chaos masking, where the secure information is being transmitted by adding in the chaotic signal directly [4]. To avoid the information being destroyed by the disturbance of the chaotic carrier waveform, and to be detectable, the amplitude of the information being sent out should be considered.

In order to implement chaos communications by making the most of such properties of chaos, two chaotic oscillators are required, one as a transmitter and the other as a receiver. At the transmitter terminal, a message signal is modulated onto a chaotic waveform carrier signal before sending out. Once the synchronized receiving oscillator has received the chaotic carrier loaded with information, the message can be decoded and recovered. The following block diagram illustrates an overview of how the chaos communication system is constructed.



Fig 1. Overview block diagram of chaotic communication system

## Methodology

- **The Rössler system**

The chaos model that would be used in this project would be an elegant, relatively simple three-dimensional chaotic system: the Rössler system, which could be demonstrated with a set of three non-linear ordinary differential equations as follow:

$$\begin{cases} \dot{x} = -y - z \\ \dot{y} = x + ay \\ \dot{z} = b + z(x - c) \end{cases} \quad (1)$$

Here,  $\begin{bmatrix} x1 \\ x2 \\ x3 \end{bmatrix} \in \mathbb{R}^3$  are dynamical variables defining the

phase space and a,b and c are parameters, where the values are defined as a=b=0.2 and c=5.7, the most commonly used parameters for Rössler system.

- **The 4<sup>th</sup> Order Runge-Kutta Method**

In order to simulate the chaotic system in MATLAB, solutions to the above mentioned Rössler system would be necessary. Thus the 4<sup>th</sup> order Runge-Kutta method was utilized to provide numerical solutions for the Rössler differential equations, as they do not have exact solutions as ordinary differential equations do [5].

- **Rössler Transmitter and Receiver**

The basic idea of the communication system is based on chaotic signal masking and recovery. At the transmitter, a chaotic signal is added to the information signal  $m(t)$ , and at the receiver the chaotic noise is being removed.

The Rössler Transmitter could be described as

$$\dot{X} = AX + f(X) + Lm(t) \quad (2)$$

$$\text{where the state vector } X = \begin{bmatrix} x_t \\ y_t \\ z_t \end{bmatrix}, \quad (3)$$

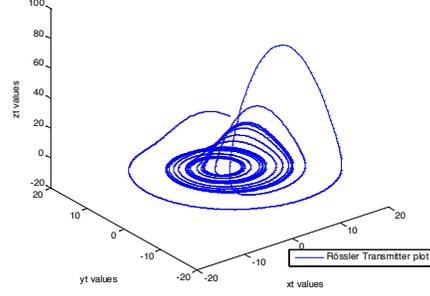
$$A = \begin{bmatrix} 0 & -1 & -1 \\ 1 & 0.2 & 0 \\ 0 & 0 & -5.7 \end{bmatrix}, \quad (4)$$

$$f(X) = \begin{bmatrix} 0 \\ 0 \\ x_t z_t + 0.2 \end{bmatrix}, \quad (5)$$

$$L = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, \quad (6)$$

$$m(t) = 10\sin(t) \quad (7)$$

$m(t)$  is signal message added into the transmitter. The plot **Fig 2**. illustrates the Rössler Transmitter with the  $m(t)$  being implemented, an initial value of (10, 10, 10) of a time step  $h=0.01$  over a time frame of [0,100].



**Fig. 2** Plot for transmitter system with implemented message

The Rössler Receiver could be described as

$$\dot{Y} = A'Y + f(Y) \quad (8)$$

$$\text{where the state vector } Y = \begin{bmatrix} x_r \\ y_r \\ z_r \end{bmatrix}, \quad (9)$$

$$A' = \begin{bmatrix} 0 & -1 & -1 \\ 1 & 0.2 & 0 \\ k1 & k2 & k3 - 5.7 \end{bmatrix}, \quad (10)$$

$$f(Y) = \begin{bmatrix} 0 \\ 0 \\ x_r z_r + 0.2 \end{bmatrix}, \quad (11)$$

$$L = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad (12)$$

$$\widehat{m}(t) = k_1 x_r + k_2 y_r + k_3 z_r + x_r z_t + x_t z_r - x_r z_r \quad (13)$$

as  $Y \rightarrow 0$

$\widehat{m}(t)$  is the estimate of the input message signal  $m(t)$ .  $k_1$ ,  $k_2$  and  $k_3$  are parameters added to the Receiver and are chosen to force  $Y \rightarrow 0$ . This is achieved by setting the eigenvalues of  $\begin{bmatrix} 0 & -1 & -1 \\ 1 & 0.2 & 0 \\ k1 & k2 & k3 - 5.7 \end{bmatrix}$  to the left half plane [6].

The calculated results for  $k_1$ ,  $k_2$  and  $k_3$  would be  $k_1= 11.24$ ,  $k_2= 2.408$ ,  $k_3=-6.2$ . The plot below demonstrated the stabilized Rössler Receiver in its three corresponding state variables  $x_r$ ,  $y_r$  and  $z_r$ . As a result of being a stabilized dynamic chaos system, the state variable would gradually going to zero.

The plot for the stabilized receiver system demonstrated below are generated under the conditions of a time step  $h=0.01$  together with an initial condition of (10, 10, 10).

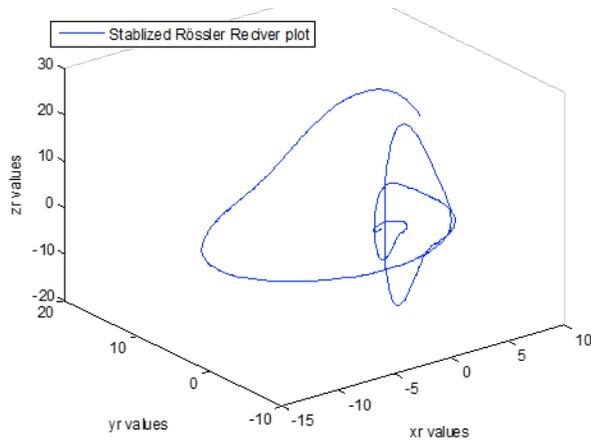


Fig. 3 3D Plot for stabilized Receiver system

In our system, the basic idea is to regenerate the message signal by restating the error system, which is the received signal at the receiver and subtract the transmitted signal to recover  $m(t)$ . This goal can be achieved as long as the Rössler Receiver could be stabilized. The below graph illustrates the approach to recover  $m(t)$ .

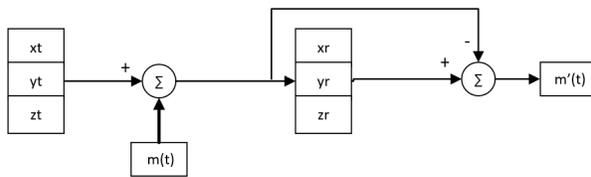


Fig. 4. Rössler communication system with system state variables

#### Recovery of the message signal

As mentioned above, once  $Y \rightarrow 0$  in the Rössler Receiver the message signal could be recovered. Based on equations (8) - (13), the estimated  $\widehat{m}(t)$  could be expressed in state variables of the Rössler Transmitter and Receiver:

$$\widehat{m}(t) = z_r - k_1 x_r - k_2 y_r - (k_3 - 5.7) z_r - x_r z_r + x_t z_t + x_r z_r$$

(14)

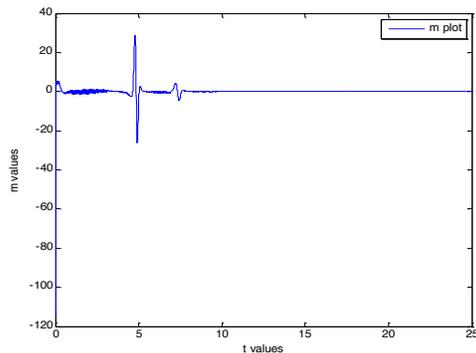


Fig. 8 Recovered message signal  $m(t)$  of time period [0,25]

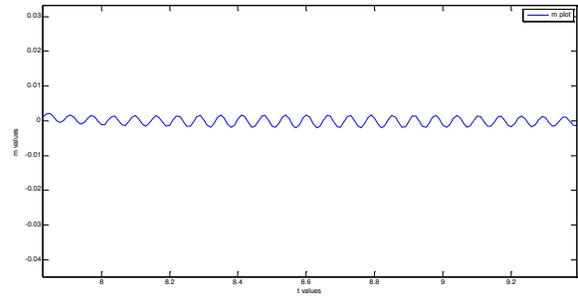


Fig. 9 Recovered message signal  $m(t)$  of time period [0, 9.4]

In the above demonstrated simulation, the initial values of the receiver is chosen as  $(0.2,0,0)$ , with the time step  $h=0.01$  results of the recovered information signal  $m(t)$ , the sine wave could be regenerated.

#### Conclusions

A chaos synchronization and secure communication method is designed and displayed. Using the Rössler communication system presented in this paper, a message embedded into the Rössler variables can be recovered at the receiver. This new way of information transmission could benefit the improvement of secure communication.

#### References

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